

NUCLEAR MAGNETIC RESONANCE (NMR)

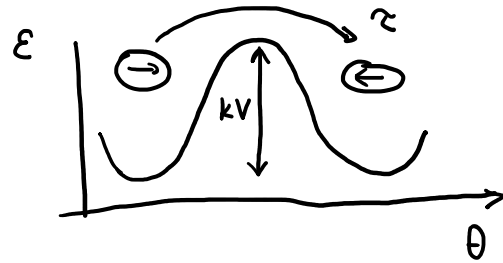


S. Parkin et al. *Science* **320**, 190 (2008)

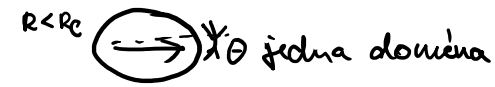
S. Parkin & S. H. Yang. *Nature Nanotechnology* **10**, 195 (2015)

EFEKTY REDUKOVANÉ DIMENZE - SUPERPARAMAGNETISMUS

3 REDUKOVANÉ DIMENZE: SUPERPARAMAGNETISMUS



častice podkrit. polom: $R_c = \frac{9\pi\sqrt{AK}}{\mu_0 M^2}$



uniax. aniz.
 $E_A = KV$
term. fl. $\sim k_B T$

mat. vlastnost ($\sim 1 \text{ ns}$)
 $\tau = \tau_0 e^{\frac{KV}{k_B T}}$
čas přechodu

měříci obno t : $t \ll \tau$ častice stabilní $\langle M \rangle = M_s$
 $t \gg \tau$ $\langle M \rangle = 0$

$\frac{KV}{k_B T} = \alpha$
 $\alpha \propto R_B^3$ blocking radius
 blocking constant
 blocking T

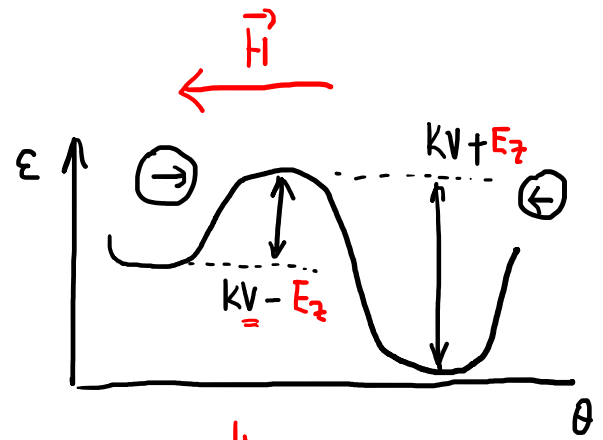
α $\begin{cases} > 25 & \text{lab. stabilita} & \tau \approx 100 \text{ s} \\ > 60 & \text{pevně drží} & \tau \sim 10^{12} \text{ let} \end{cases}$

Table 8.5. Superparamagnetic relaxation times for cobalt particles

Radius (μm)	Temperature (K)	Relaxation time
3.5	260	332 s
3.5	300	10 s
3.5	340	0.6 s
3.5	380	76 ms
3.0	300	1.9 ms
4.0	300	223 h
5.0	300	$L \times 10^{12}$ y

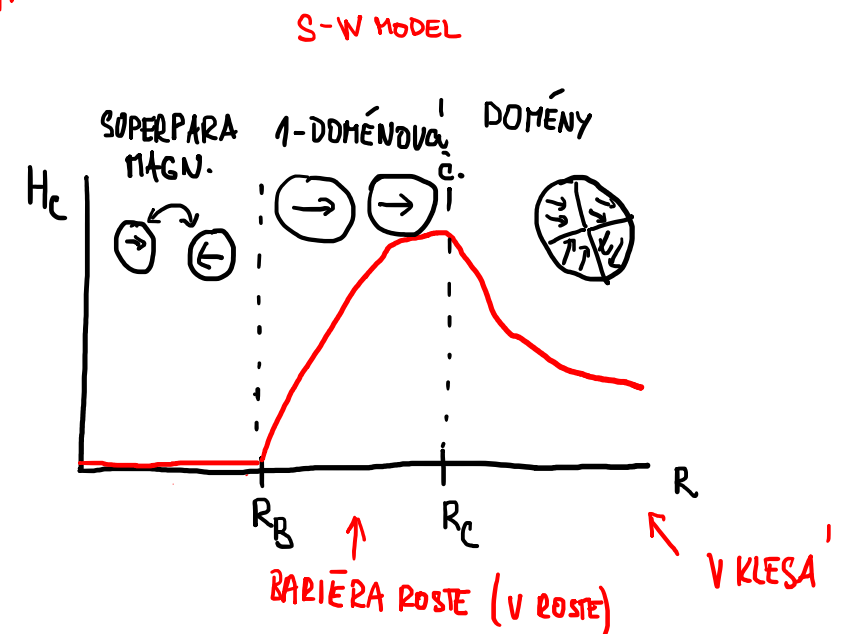
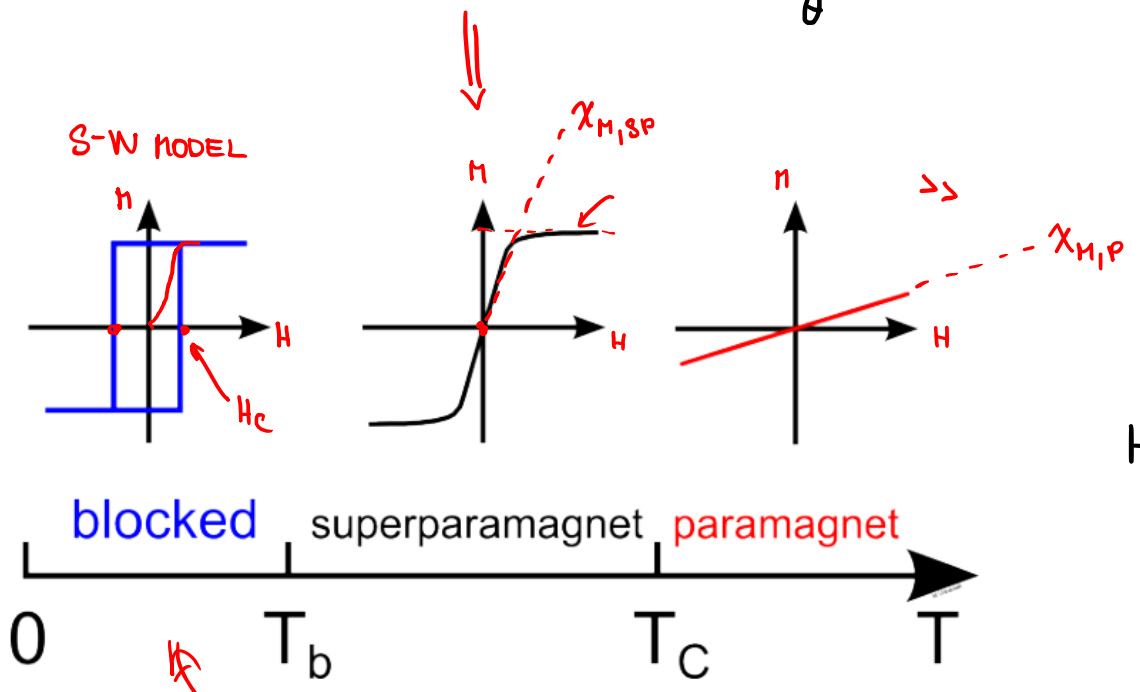
EFEKTY REDUKOVANÉ DIMENZE - SUPERPARAMAGNETISMUS

Série částie:



$$E_z = -\mu_0 M H \cos \theta$$

$$\alpha \propto \frac{r^3}{V}, \frac{1}{T}$$

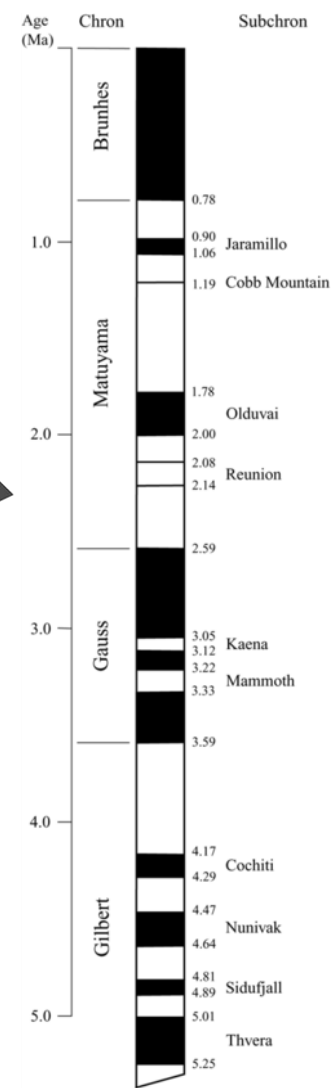
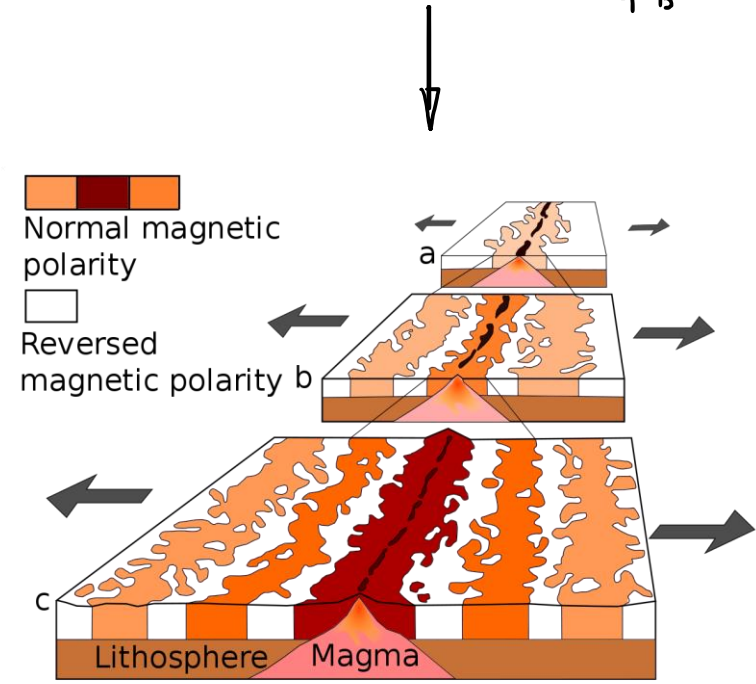


EFEKTY REDUKOVANÉ DIMENZE - SUPERPARAMAGNETISMUS

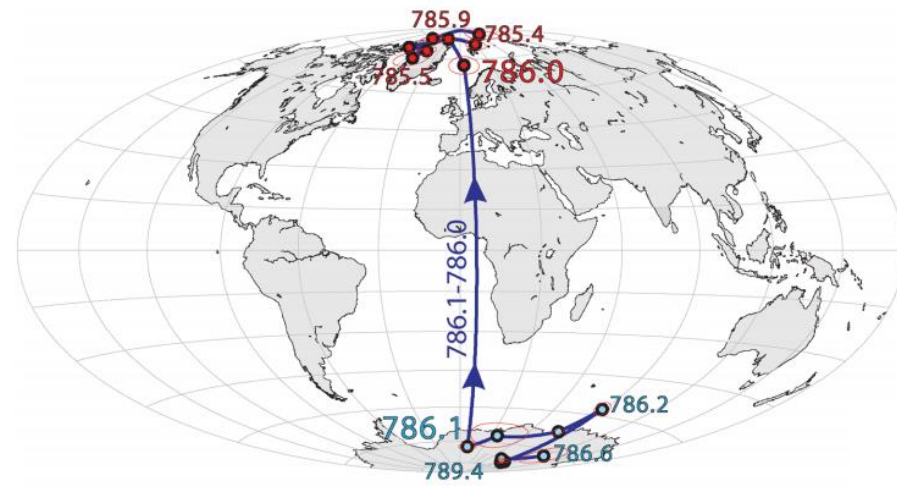
ČÁSTICE HEKATITU (OXID Fe) V LÁVĚ

SUPERPARAMG. $T > T_c, T_B$

$T \downarrow$
 \rightarrow FEROMG. ADOMÉNOVA'Č.



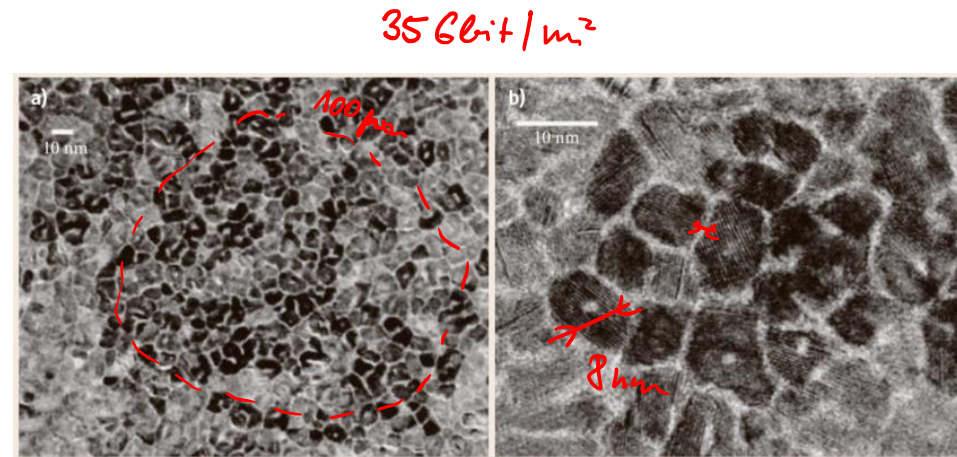
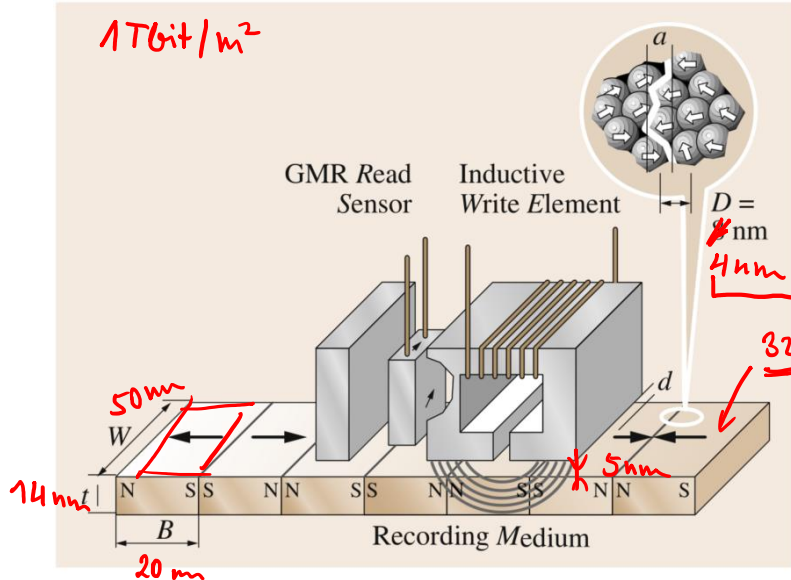
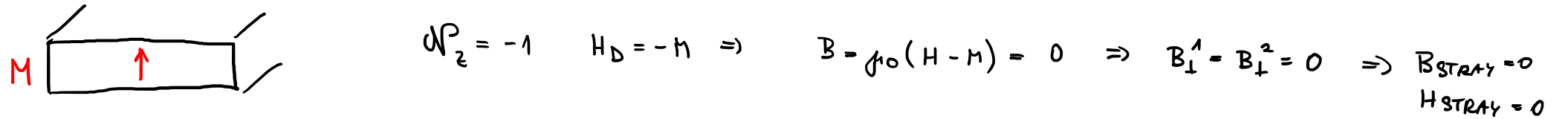
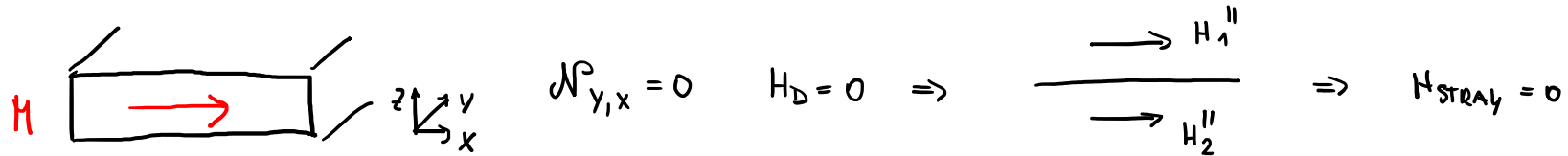
PŘEKMIT MG. PÓLU ZEMĚ



Sagnotti et al., Geophys. J. Int. (2014) 199, 1110–1124

EFEKTY REDUKOVANÉ DIMENZE - TENKÉ VRSTVY

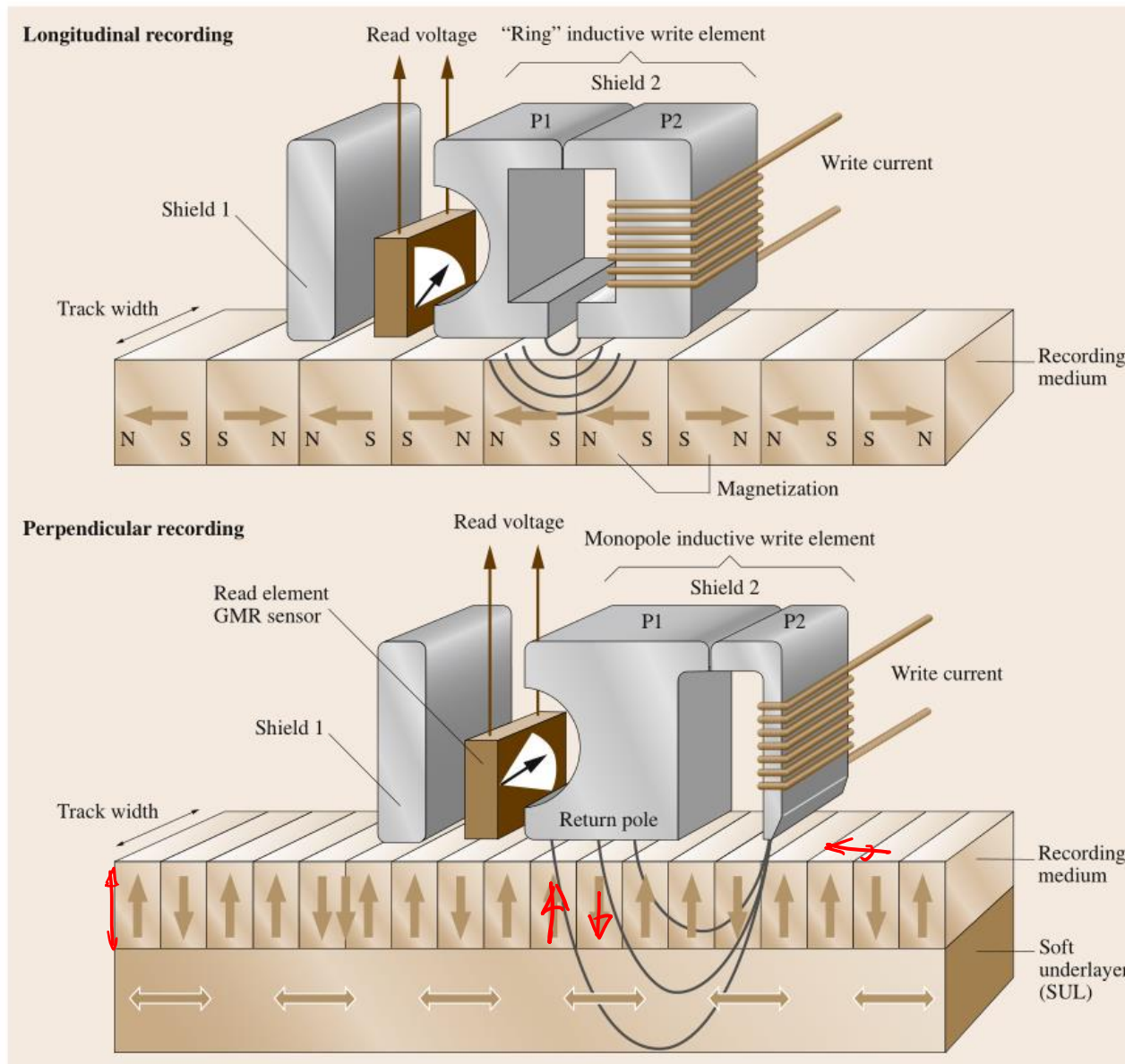
2D OMEZENÍ : TENKÉ VRSTVY



https://link.springer.com/chapter/10.1007/978-3-319-48933-9_49

S. Kasap, P. Capper (Eds.), Springer Handbook of Electronic and Photonic Materials

EFEKTY REDUKOVANÉ DIMENZE - TENKÉ VRSTVY



https://link.springer.com/chapter/10.1007/978-3-319-48933-9_49

S. Kasap, P. Capper (Eds.), Springer Handbook of Electronic and Photonic Materials

EFEKTY REDUKOVANÉ DIMENZE - TENKÉ VRSTVY

2D OMEZENÍ : TENKÉ VRSTVY

ANISOTROPIE: "3s"

SHAPE

$$\begin{aligned} \mathcal{P}_{x1y} &= 0 \\ \mathcal{P}_z &= -1 \end{aligned}$$



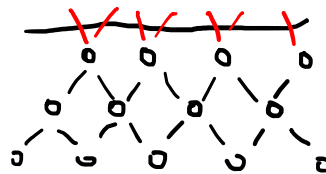
$$E_A = K_u \sin^2 \theta$$

$$K_u = -\frac{1}{2} \mu_0 M_s^2$$

⇒ inplane

$$K_{SH} \sim -1 \text{ MJ/m}^3$$

SURFACE

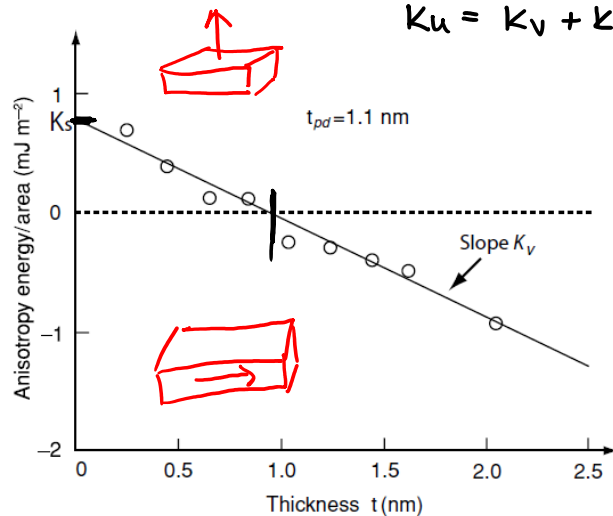


$$K_u = K_s < 0$$

OUT-OF PLANE

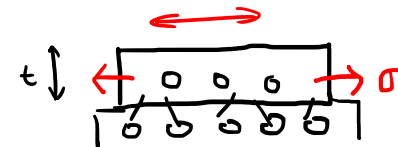
$$K_s \sim 1 \text{ MJ/m}^2$$

$$K_u = K_v + K_s / t$$



STRAIN

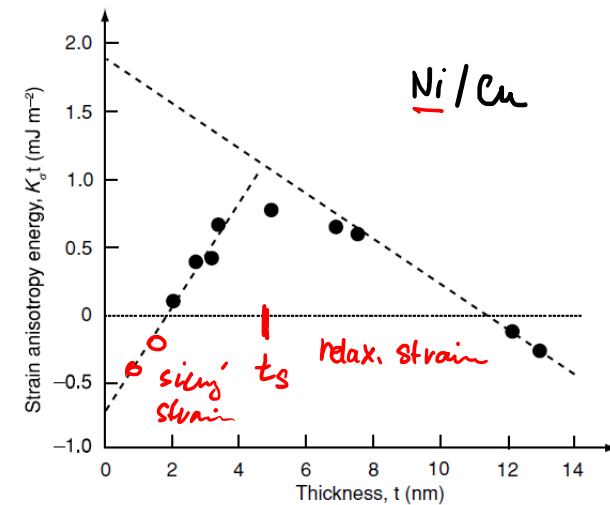
R. Jungblut, JAP 75 6424 (1994)



$$K_\sigma \propto \lambda_s \sigma \propto \epsilon_u t_s / t \propto 1/t$$

SPONTANĚNÍ
MAGNETOSTRIKCE

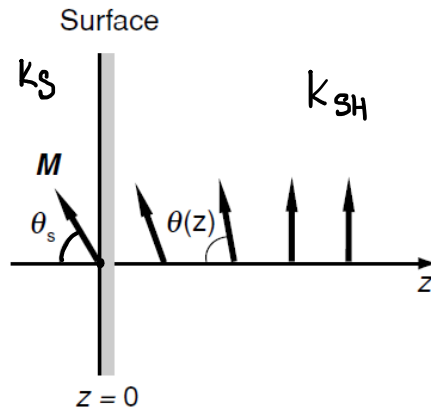
$$K_\sigma \sim -100 \text{ kJ/m}^3$$



EFEKTY REDUKOVANÉ DIMENZE - TENKÉ VRSTVY

2D OMEZENÍ : TENKÉ VRSTVY

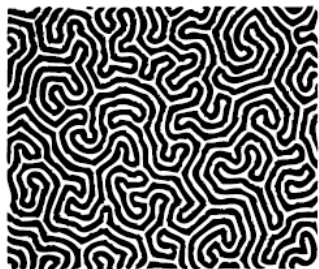
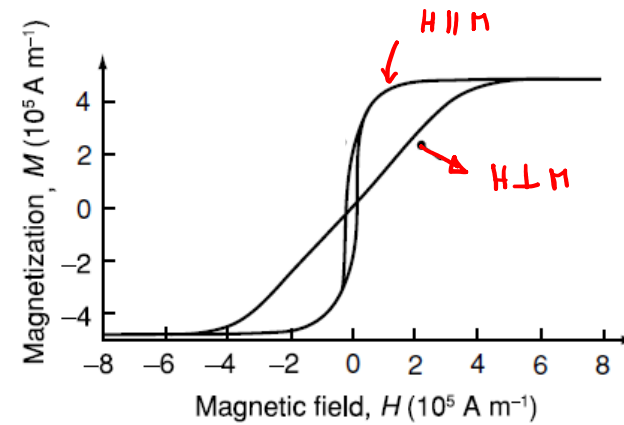
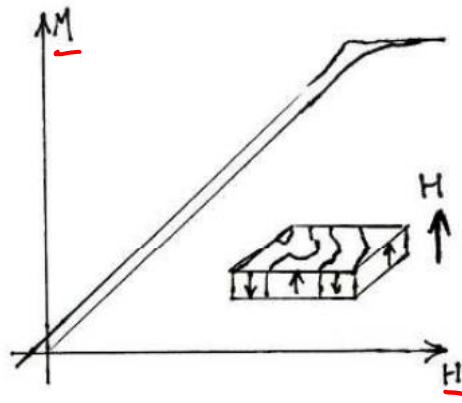
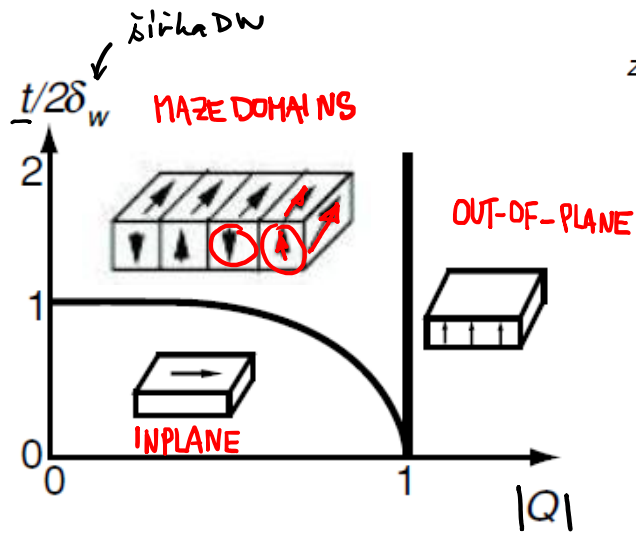
ANISOTROPIE :



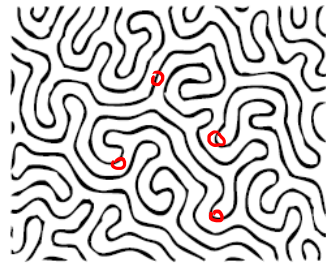
$\theta(z) = 2 \tan^{-1} \left[e^{\pi(z-z_0)/\delta_{DW}} \right]$ ← tloušťka

$z_0 : \theta(z=z_0) = \theta_s$

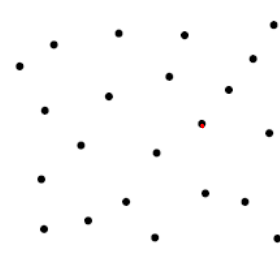
$Q = - \frac{k_{\perp}}{k_{SH}}$ quality factor



$H=0$



$\odot H$



$\odot H$

BUBBLE DOMAINS



EFEKTY REDUKOVANÉ DIMENZE - BUBBLE DOMAINS

2D OMEZENÍ : TENKÉ VRSTVY

BUBBLE MEMORY
(BELLABS, IBM...) $\bar{7}_0, \bar{8}_0$

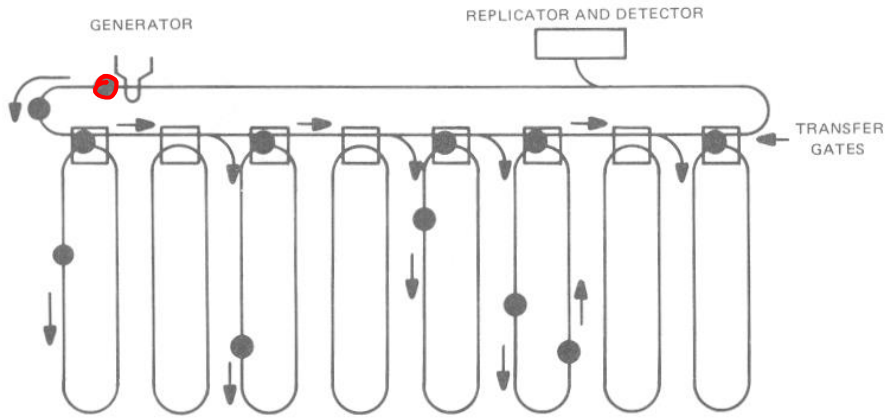
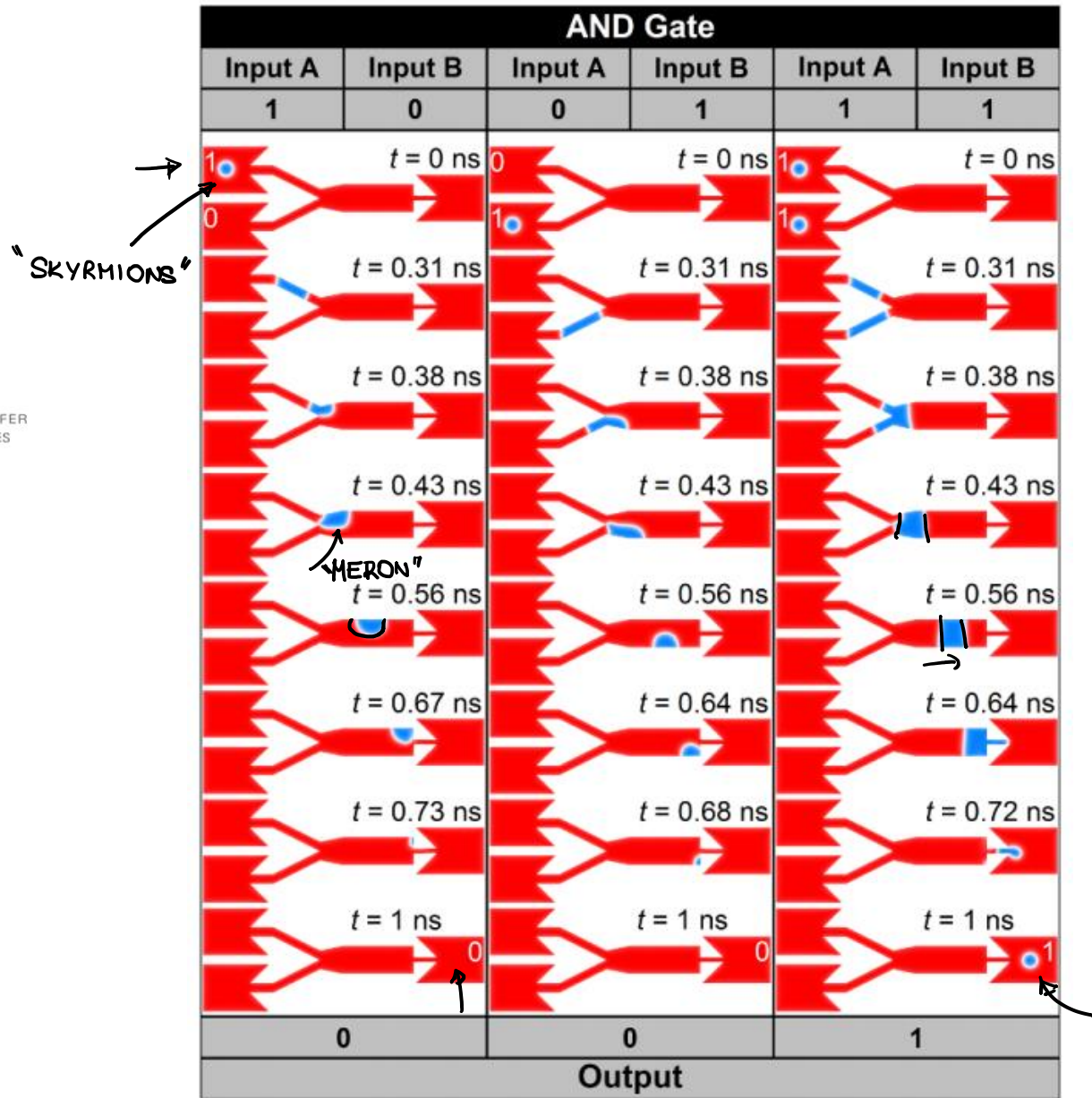
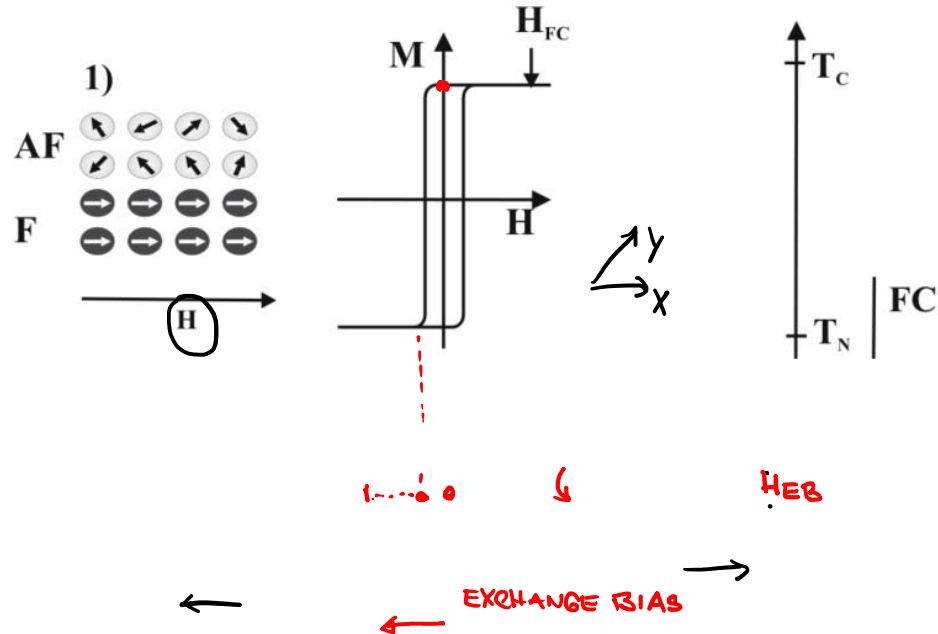


FIGURE 5. ARCHITECTURE USING MAJOR AND MINOR LOOPS



EFEKTY REDUKOVANÉ DIMENZE - EXCHANGE BIAS

2D OMEZENÍ : TENKÉ VRSTVY
HETEROSTRUKTURY :



• $H_x \parallel \vec{L}$

$$E_x = -\mu_0 n H_x \cos \theta - \underbrace{k_{EB} \cos^2 \theta}_{\frac{\sigma_{EX}}{t}} + K_u \sin^2 \theta$$

UNIDIRECTIONAL UNIAXIAL

}

$$-\mu_0 M H'_x \cos \theta$$

$$H'_x = H_x + H_{EX}$$

$$H_{EX} = \frac{\sigma_{EX}}{\mu_0 M t}$$

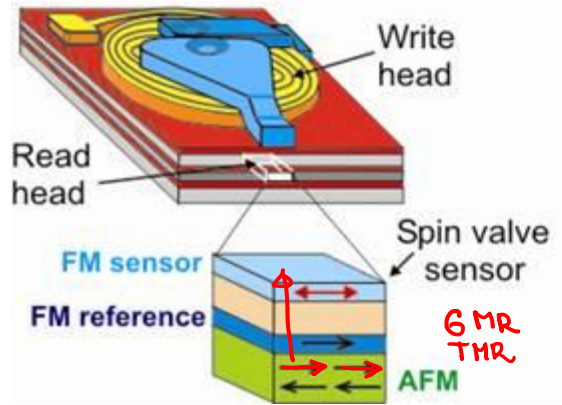
• $H_y \perp \vec{L}$

EFEKTY REDUKOVANÉ DIMENZE - EXCHANGE BIAS

2D OMEZENÍ : TENKÉ VRSTVY

HETEROSTRUKTURY :

Magnetic recording head

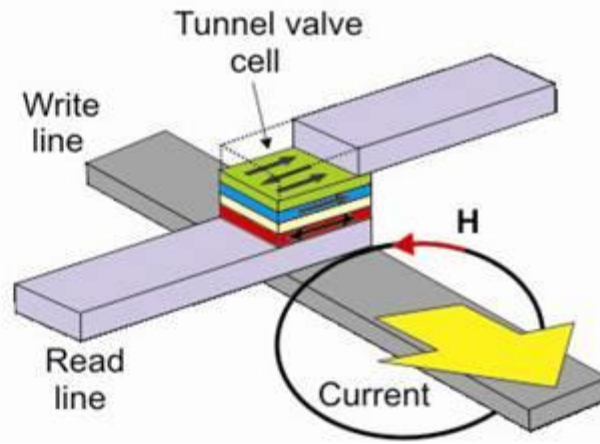


0 ↔ 1

MRAM

Magnetic memory cell

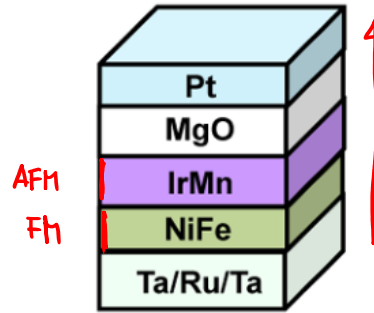
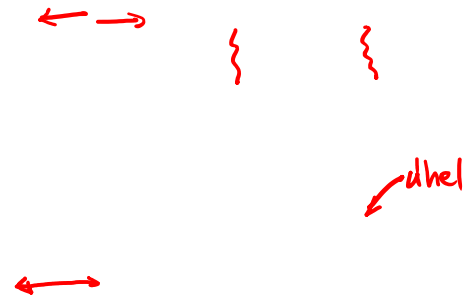
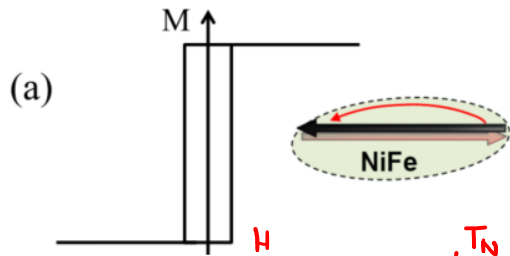
RAM + GMR THR



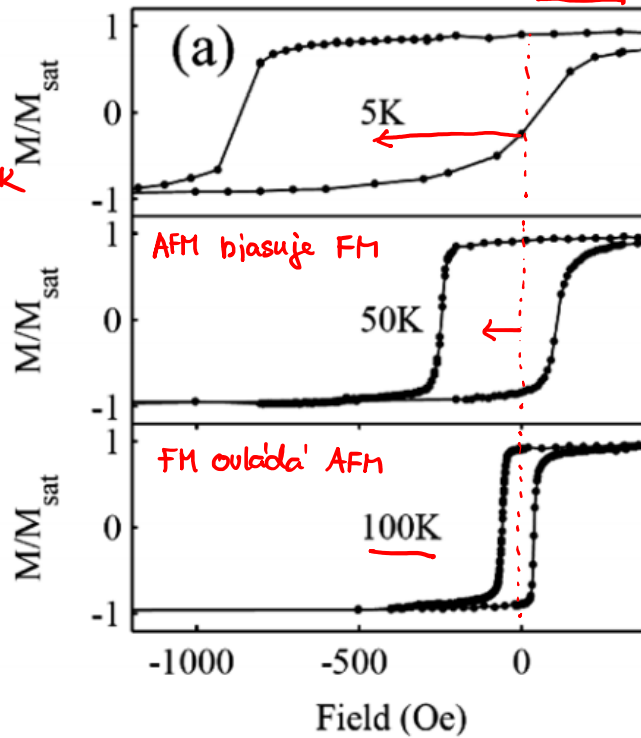
EFEKTY REDUKOVANÉ DIMENZE - EXCHANGE BIAS

2D OMEZENÍ : TENKÉ VRSTVY
 HETEROSTRUKTURY :

→ EXCHANGE BIAS OVLADÁNÍ AFM



IrMn(3 nm) SQUID

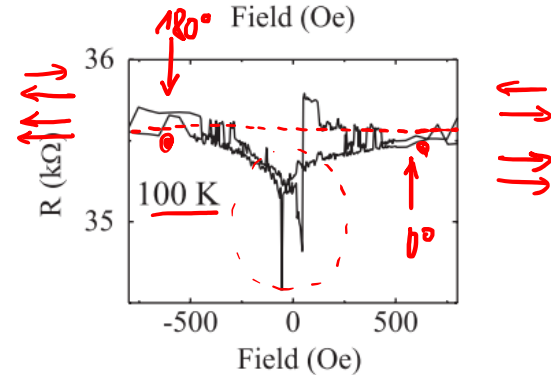
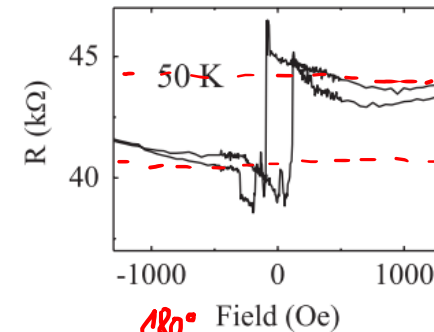
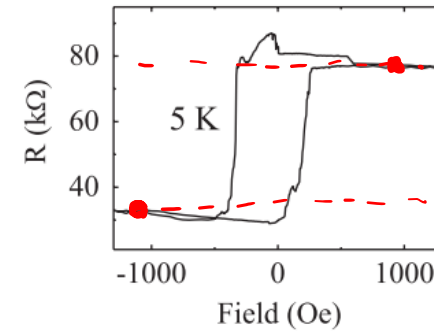


TUNNELLING ANISOTROPIC
 MAGNETORESISTANCE

$$R(0^\circ) = R(180^\circ) \neq R(90^\circ)$$

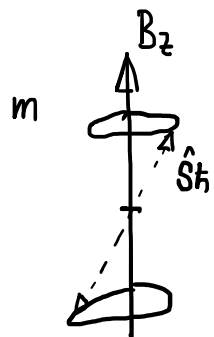
IrMn (3 nm)

6MR
 MLD
 AMR



MAGNETICKÁ REZONANCE

KVANTOVĚ

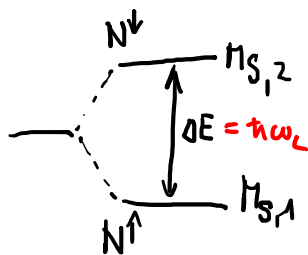


$$\vec{M} = \gamma \hbar \hat{S}$$

$$\hat{H} = -\vec{m} \cdot \vec{B}_0 = -\gamma \hbar \hat{S}_z B_0$$

$$E = \gamma \hbar B_0 m_s \quad m_s = s, s-1, \dots, -s$$

$$\Delta E = \hbar \omega_L \quad \omega_L = \gamma B_0 = \frac{e g}{2m} B_0$$



PŘECHOD:

$$\langle M_{S,2} | \hat{H} | M_{S,1} \rangle$$

← také $\frac{\mu_B}{\hbar}$

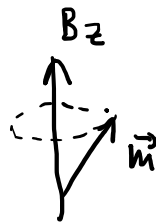
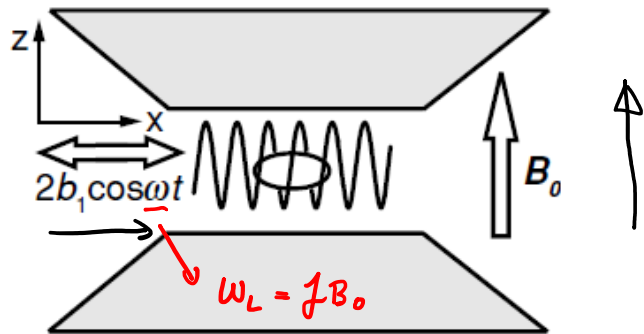
$$\hat{H} \propto \hat{S}_z \rightarrow \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

\Rightarrow čistě stavů $\Rightarrow 0$

$$\hat{H} \propto \hat{S}_x$$

$$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

"DIPOLAR SELECTION RULES"



KLASICKY

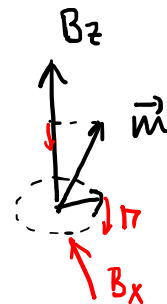
$$\vec{\Gamma} = \vec{m} \times \vec{B}_0$$

torque = změna ang. mom. \vec{L} : $\vec{m} = \gamma \vec{L}$

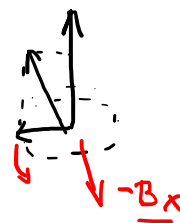
$$\frac{d\vec{m}}{dt} = \dot{\vec{m}} = \gamma \vec{m} \times \vec{B}_0 \rightarrow$$

řešení ve složkách $\rightarrow \omega_L = \gamma B_0$

$m_z = \text{konst.}$



B musí být \perp na \hat{z}



$\Rightarrow B_x$ harmonický kmitá na ω_L
rezonance

MAGNETICKA' REZONANCE

Numbers:

$$f_L = \frac{\omega_L}{2\pi} = \frac{e\hbar}{2\pi m} B_0$$

pro e^- : $g \sim 2$ (value)
 $1T \dots 28 \text{ GHz}$

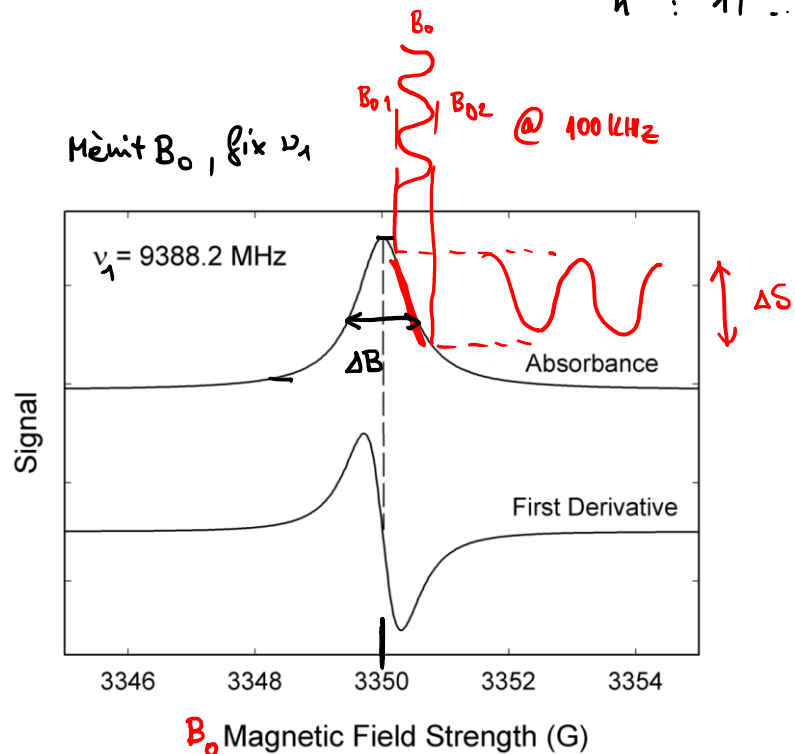
pro p^+ : $1T \dots 43 \text{ MHz}$

h^0 : $1T \dots 29 \text{ MHz}$

$$\left(\frac{N^\downarrow}{N^\uparrow}\right)_0 \sim e^{-\frac{\hbar\omega}{kT}}$$

$$\rho = \frac{N^\uparrow - N^\downarrow}{N^\uparrow + N^\downarrow} \sim \underline{10^{-3}} \text{ @ } 300 \text{ mT RT}$$

Meit B_0 , fix ν_1



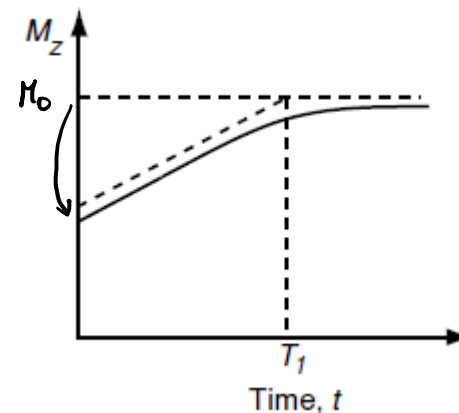
RELAXACNI CAS (LONGITUDINALNI)
 SPIN-LATTICE RELAX. TIME

$$M_z = 1 - e^{-t/T_1}$$

$$\Delta t \Delta E \sim \hbar$$

$$T_1 \Delta B \sim \frac{\hbar}{\mu_B g}$$

$$\Delta B \sim 1 \text{ mT} \rightarrow T_1 \sim \underline{5 \text{ ns}}$$



\rightarrow preference $L=0, S \neq 0 \Rightarrow J=S \Rightarrow$ small coupling to lattice

$T_1 \uparrow \Delta B \downarrow$ pozorovatelné

MAGNETICKA' REZONANCE

REZONANCE

PARAMAGNETICKA' (ELEKTRONOVA')

$$E = g \mu_B B m_J$$

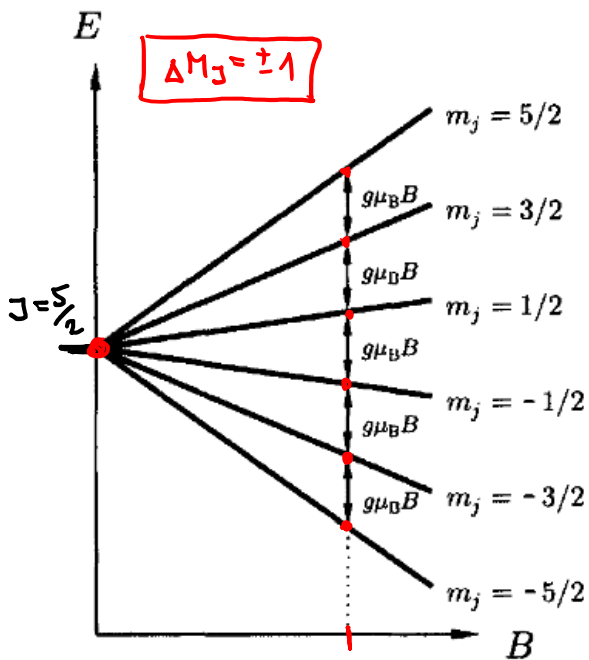
→ často $L=0$

$$g = \frac{S(S+1) - L(L+1)}{2J(J+1)} + \frac{3}{2} = 2 = g_e$$

Pr. $Mn^{2+} (3d^5)$: $l=2$

m_l	-2	-1	0	1	2
	↑	↑	↑	↑	↑

$L=0$ $S=5 \cdot \frac{1}{2} = \frac{5}{2}$
 $J=?$ $|L-S| \leq J \leq L+S$
 $J = 5/2$



$$\hbar\omega = E = g \mu_B B$$

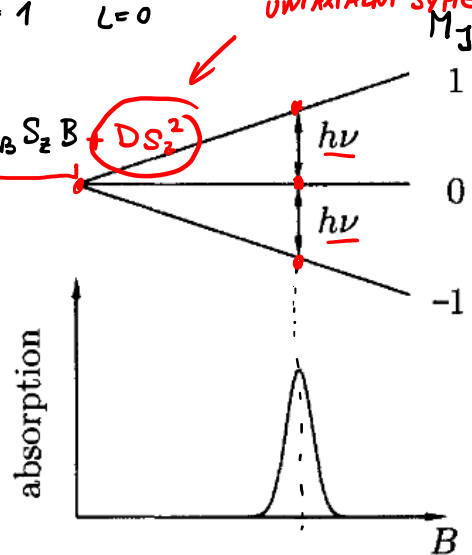
$$m_J = -J, -J+1, \dots, J$$

→ Efect krystal. pole:

pro $J=S=1$ $L=0$

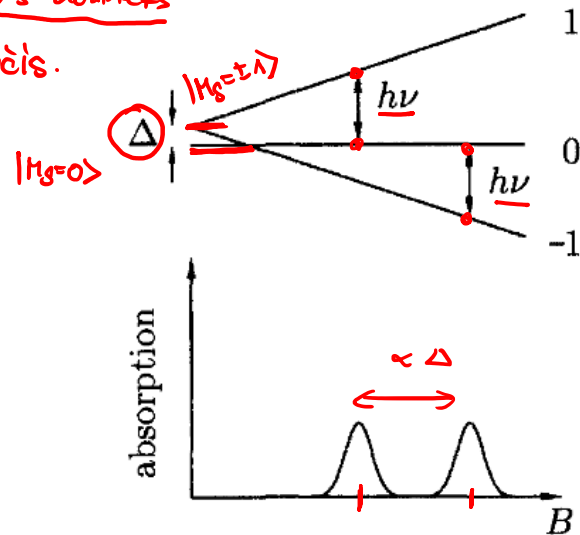
UNIAXIÁLNI SYMETRIE KRYS. POLE

$$\hat{H}_{EF} = -g_{EF} \mu_B S_z B + D S_z^2$$



Kramer's doublets

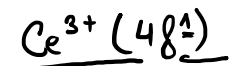
J: oddis.



MAGNETICKA' REZONANCE

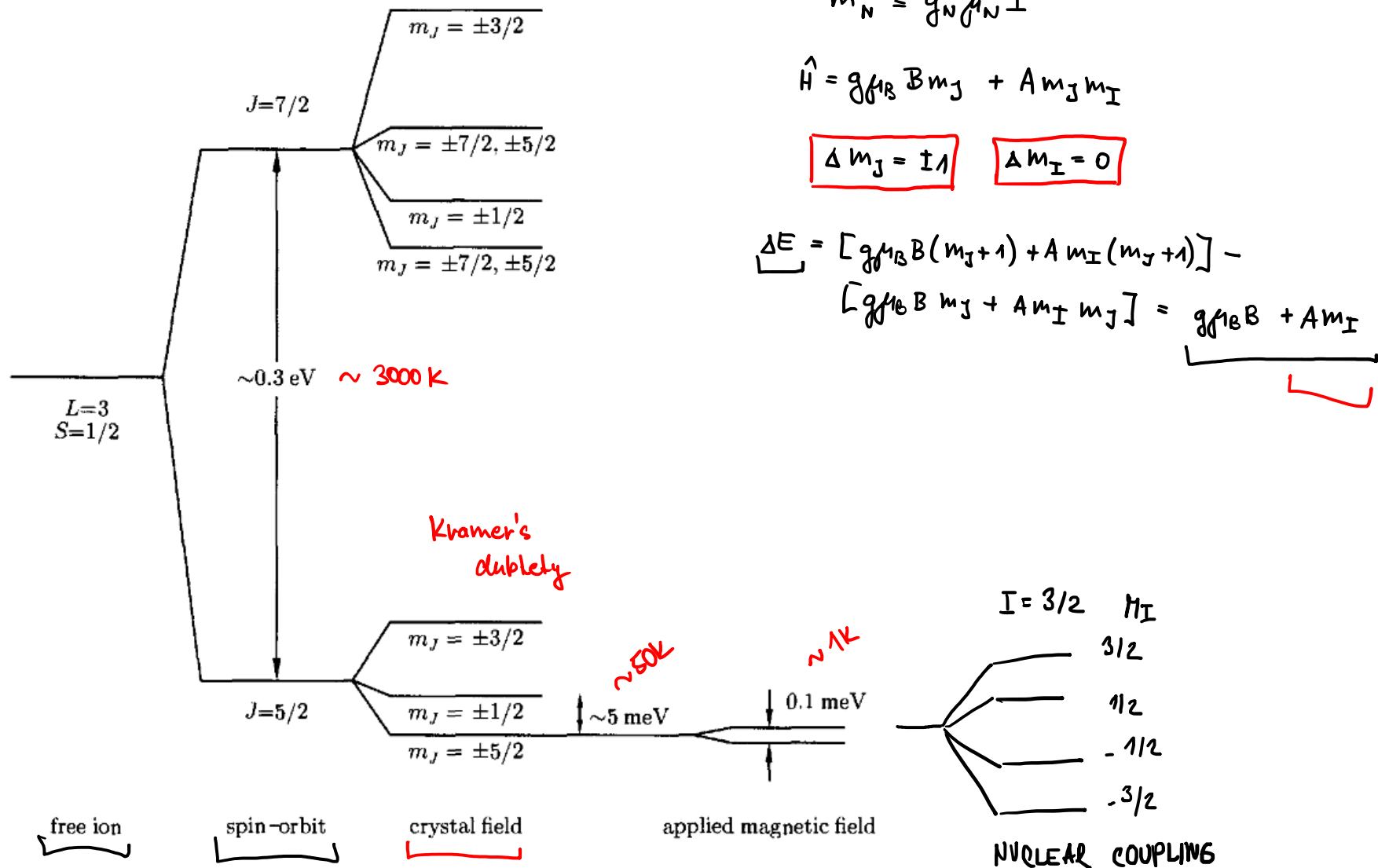
REZONANCE

PARAMAGNETICKA'
(ELEKTRONOVA')



$L=3 \quad S=1/2$

$J = \frac{5}{2}, \frac{7}{2}$



NUKLEARNI' MOMENT:

$\hbar I$

$m_N = g_N \mu_N I$

$\hat{H} = g \mu_B B m_J + A m_J m_I$

$\Delta m_J = \pm 1$ $\Delta m_I = 0$

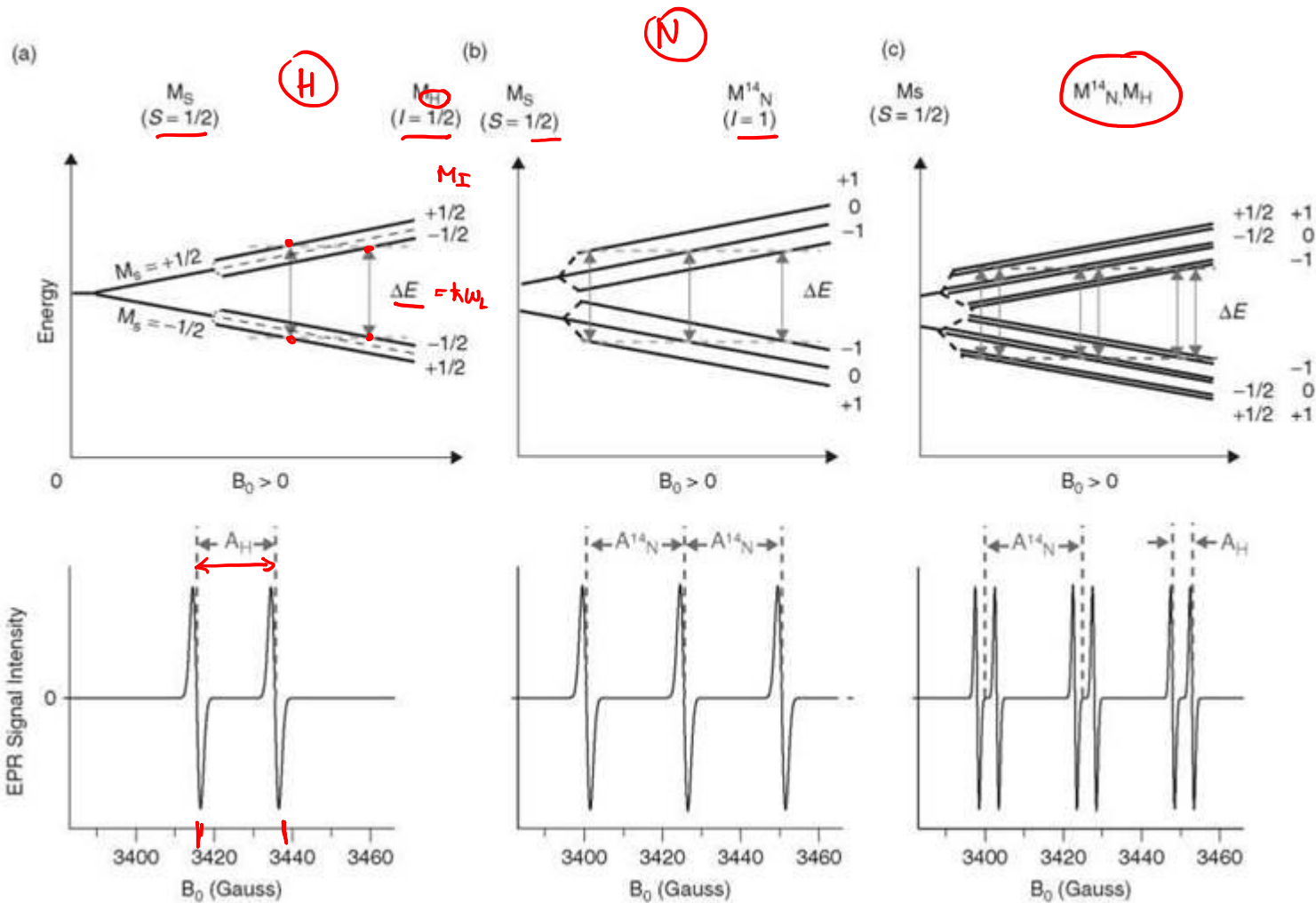
$\Delta E = [g \mu_B B (m_J + 1) + A m_I (m_J + 1)] - [g \mu_B B m_J + A m_I m_J] = g \mu_B B + A m_I$

MAGNETICKA' REZONANCE

REZONANCE

PARAMAGNETICKA'
(ELEKTRONOVA')

($1s^2 2s^2 2p$)



MAGNETICKÁ REZONANCE

REZONANCE FEROMAGNETICKÁ

→ spin dominantní přisp. v kovech

VNITŘÍ FM: $H = H' + H_D + H_A$

→ rezonance $H' = H_0 \hat{z}$

$M = M_s \hat{z} + m(t)$ $m(t) = m_0 e^{i\omega t}$ in plane

$H_D = -\mathcal{D}P M$ $\mathcal{D}P = \begin{pmatrix} \mathcal{D}P_x & 0 & 0 \\ 0 & \mathcal{D}P_y & 0 \\ 0 & 0 & \mathcal{D}P_z \end{pmatrix}$ $\left(H_A = -\frac{2k_1}{M} \right)$

$M \equiv M_z$
 $H_D = -[\mathcal{D}P_x m_x, \mathcal{D}P_y m_y, \mathcal{D}P_z (m_z + M_s)]$
 $\vec{H} = H_0 + H' = \dots$ $\vec{H} = (m_x, m_y, M)$

$B_0' = \mu_0 H_0'$ *vnější pole*

$\nu = \frac{\omega_L}{2\pi} = \frac{\gamma B_0}{2\pi} \sim \frac{0.3T}{2\pi} \sim 10 \text{ GHz}$ jako ESR

pro m: $\dot{m}_x = i\omega m_x = \mu_0 \gamma (m_y H_z - M H_y) = \mu_0 \gamma [H_0' + (\mathcal{D}P_y - \mathcal{D}P_z) M] m_y$ $[J_1]$

$\dot{m}_y = i\omega m_y = -\mu_0 \gamma [H_0' + (\mathcal{D}P_x - \mathcal{D}P_z) M] m_x$ $[J_2]$

$\begin{bmatrix} i\omega & -[J_1] \\ [J_2] & i\omega \end{bmatrix} = 0 \Rightarrow \omega^2 = \mu_0^2 \gamma^2 [H_0' + (\mathcal{D}P_x - \mathcal{D}P_z) M] [H_0' + (\mathcal{D}P_y - \mathcal{D}P_z) M]$

pro kouli: $\mathcal{D}P_{x,y,z} = 1/3$ $\omega = \mu_0 \gamma H_0'$ *Kittel res* H_A

$\begin{matrix} z \\ \uparrow H \\ \text{---} M \\ \text{---} x \end{matrix}$ $\mathcal{D}P_z = 1, \mathcal{D}P_{x,y} = 0 \Rightarrow \omega = \mu_0 \gamma (H_0' - M)$

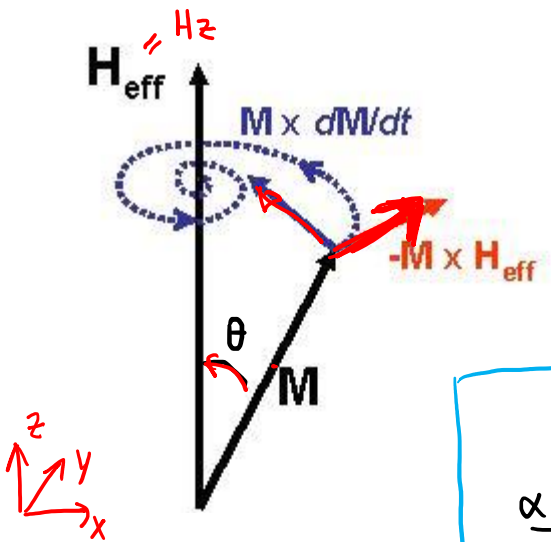
$\begin{matrix} z \\ \uparrow H \uparrow M \\ \text{---} x \end{matrix}$ $\mathcal{D}P_x = 1, \mathcal{D}P_{y,z} = 0 \Rightarrow \omega = \mu_0 \gamma \sqrt{H_0' (H_0' + M)}$

MAGNETICKÁ REZONANCE

REZONANCE FEROMAGNETICKÁ S DAMPINGEM (TLUMENÍ)

$$\dot{\vec{M}} = \mu_0 \gamma \vec{M} \times \vec{H} - \gamma \frac{\lambda}{M} \vec{M} \times (\vec{M} \times \vec{H}) \mu_0$$

$$\dot{\vec{M}} = \mu \gamma \vec{M} \times \vec{H} - \frac{\alpha}{M} \vec{M} \times \dot{\vec{M}} \quad \alpha \text{ DAMPING KONST.}$$



$\alpha = 0$

$$\dot{M}_x = \mu_0 \gamma M_y H_z \quad \dot{M}_y = -\mu_0 \gamma M_x H_z \quad \dot{M}_z = 0$$

$$\ddot{M}_x = \mu_0 \gamma H_z \dot{M}_y = -\underbrace{\mu_0^2 \gamma^2 H_z^2}_{\omega_0^2} M_x$$

$\omega_0 = \mu_0 \gamma H_z$

$$M_x = M_s e^{i\omega t} \sin \theta$$

$$M_y = i e^{i\omega t} \sin \theta$$

$$M_z = M_s \cos \theta = \text{konst.}$$

$\alpha \neq 0$

$$\dot{M}_x = \omega'_0 \left[M_y - \alpha \frac{M_x M_z}{M_s} \right] \quad \& \quad \dot{M}_z \neq 0 \Rightarrow \theta(t)$$

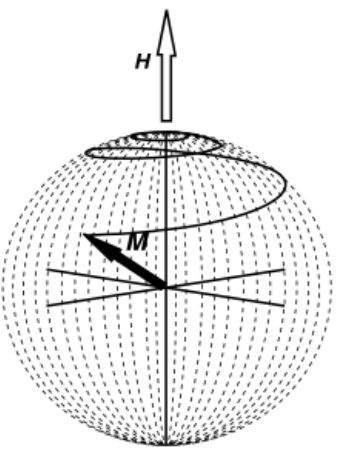
$\omega'_0 = \frac{\omega_0}{1 + \alpha^2}$ *frekv. ↓ s α ↑*

$$\dot{M}_x = i\omega M_s e^{i\omega t} \sin \theta + M_s e^{i\omega t} \cos \theta \cdot \dot{\theta} = \omega M_y + \frac{M_z M_x}{M_s \sin \theta} \dot{\theta}$$

$\Rightarrow \omega = \omega'_0$ skutečné provedení na ω'_0

$$\Rightarrow \dot{\theta} = -\omega'_0 \alpha \sin \theta$$

\rightarrow kam \vec{M} odchází? "SPIN PUMPING"



MAGNETICKÁ REZONANCE

REZONANCE ANTIFEROMAGNETICKÁ

$$H_1^z = H_A + \lambda M$$

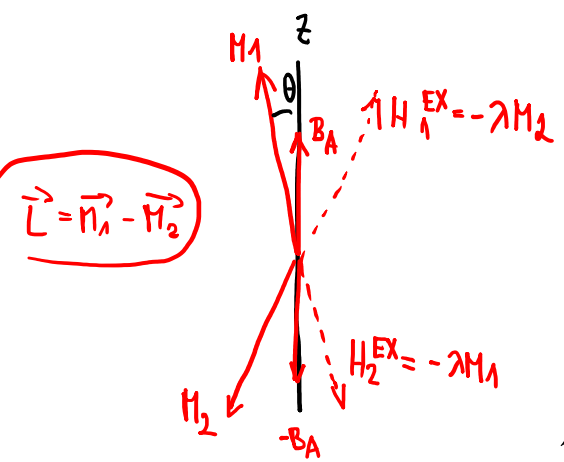
$$H_1 = H_A - \lambda M_2$$

$$M_1^z = M \quad M_2^z = -M$$

$$H_2 = -H_A - \lambda M_1$$

$$H_2^z = -H_A - \lambda M$$

$$H_A = \frac{2K}{M} \quad E_A = K \sin^2 \theta$$



$$\begin{cases} \oplus \left\{ \begin{aligned} \dot{M}_1^x &= \gamma \mu_0 [M_1^y (\lambda M + H_A) - M (-\lambda M_2^y)] \\ \dot{M}_1^y &= \gamma \mu_0 [M (-\lambda M_2^x) - M_1^x (\lambda M + H_A)] \end{aligned} \right. \\ \oplus \left\{ \begin{aligned} \dot{M}_2^x &= \gamma \mu_0 [M_2^y (-\lambda M - H_A) - (-M) (-\lambda M_1^y)] \\ \dot{M}_2^y &= \gamma \mu_0 [(-M) (-\lambda M_1^x) - M_2^x (-\lambda M - H_A)] \end{aligned} \right. \end{cases}$$

$$M_1^+ = M_1^x + i M_1^y \quad M_2^+ = M_2^x + i M_2^y$$

$$M_1^+ \rightarrow M_1^+ e^{-i\omega t}$$

$$\dot{M}_1^+ = -i\omega t M_1^+ = -i \gamma \mu_0 [M_1^+ (H_A + \lambda M) + M_2^+ (\lambda M)]$$

(zkusit doplnit M_1^+ a vyjede to)

$$\dot{M}_2^+ = -i\omega t M_2^+ = i \gamma \mu_0 [M_2^+ (H_A + \lambda M) + M_1^+ (\lambda M)]$$

$$\lambda M = H_E$$

$$\rightarrow \text{řešení existuje, pokud } \begin{vmatrix} \gamma \mu_0 (H_A + H_E) - \omega & \gamma \mu_0 H_E \\ \gamma \mu_0 H_E & \gamma \mu_0 (H_E + H_A) + \omega \end{vmatrix} = 0$$

$$(A-B)(A+B) = A^2 - B^2$$

$$\Rightarrow \gamma^2 \mu_0^2 (H_E + H_A)^2 - \omega^2 - \gamma^2 \mu_0^2 H_E^2 = 0$$

$$\omega^2 = \gamma^2 \mu_0^2 [(H_E + H_A)^2 - H_E^2] = \gamma^2 \mu_0^2 [H_A^2 + 2H_A H_E] \Rightarrow$$

$$\omega = \gamma \mu_0 \sqrt{H_A (H_A + 2H_E)}$$

$$\approx 54 \text{ T} / \mu_0 + \gamma \mu_0 H_0$$

1 THz

1 T / μ_0

→ závisí, zda jsme pod H_{SF} , nebo nad ní
 spin flop

MAGNETICKÁ REZONANCE

REZONANCE **NUKLEÁRNÍ** → podobné jako ESR: $g_N \sim 5,58$ $g_P \sim -3,83$ $\mu_N = \frac{e\hbar}{2m_p} \ll \mu_B$

$$\rightarrow \frac{\omega_L}{2\pi} \sim \begin{array}{l} 10-15 \text{ MHz} / 0.3 \text{ T} \\ 500-800 \text{ MHz} / 12-20 \text{ T} \end{array}$$

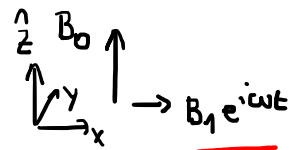
⇒ vlnová (ESR) → RF cívký (NMR)

$$\hat{H}_N = -g_N \mu_N \hat{I} \cdot B_{HF} + \dots$$

B_0 + coupling na e^- spin (knight's shift ... pro vodivostní e^-)
+ chemical shift (molekulární pole)

MAGNETICKÁ REZONANCE

RELAXACE



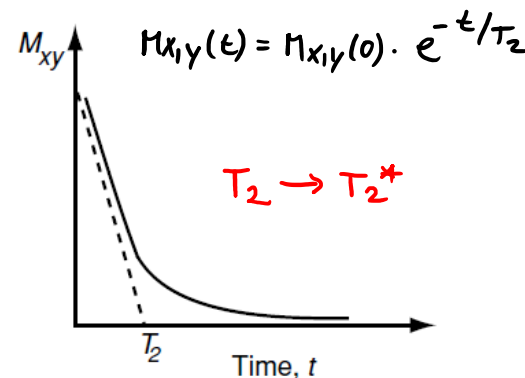
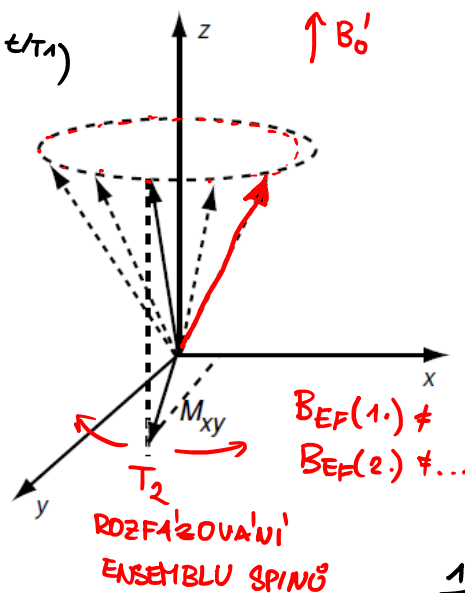
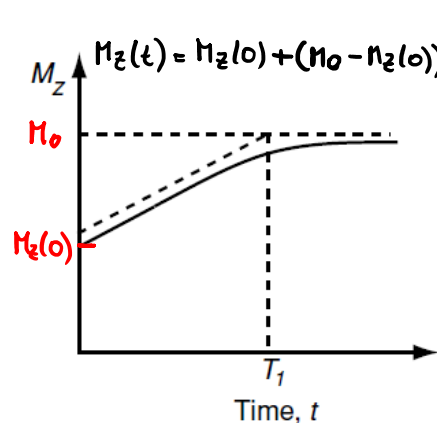
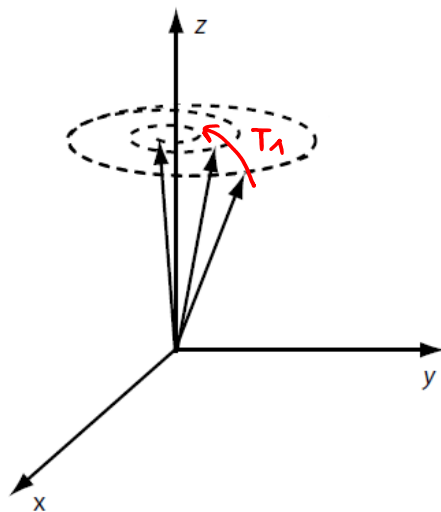
$$\dot{M}_z = \gamma(M \times B)_z + \frac{M_0 - M_z}{T_1} \quad M_0 - \text{rovnovážná pro } B_1 = 0$$

$$\dot{M}_x = \gamma(M \times B)_x - \frac{M_x}{T_2}$$

LONGITUDINÁLNÍ RELAXAČNÍ ČAS (SPIN-TO-LATTICE)

$$\dot{M}_y = \gamma(M \times B)_y - \frac{M_y}{T_2}$$

TRANSVERZÁLNÍ REL. ČAS (SPIN-TO-SPIN) - DEPHASING TIME



$T_1 > T_2$ pro NMR
 $T_1 \sim T_2$ polovod. a spiny

ČASOVĚ PROMĚNNÉ POLE B_{EF}
 A SPIN-SPIN VĚMĚNA

$\frac{1}{T_2^*} = \frac{1}{T_2} + \frac{1}{T_2^{INH.}}$

PROSTOROVÁ NEHOMOGEN. B_{EF}
 (B_0')
 (CHEMICAL SHIFTS)

MAGNETICKÁ REZONANCE

PULZNI NMR | ESR...

procesy



$M_x \sim e^{i\omega t}$
 φ
 B_1

$\varphi = \int \omega dt$

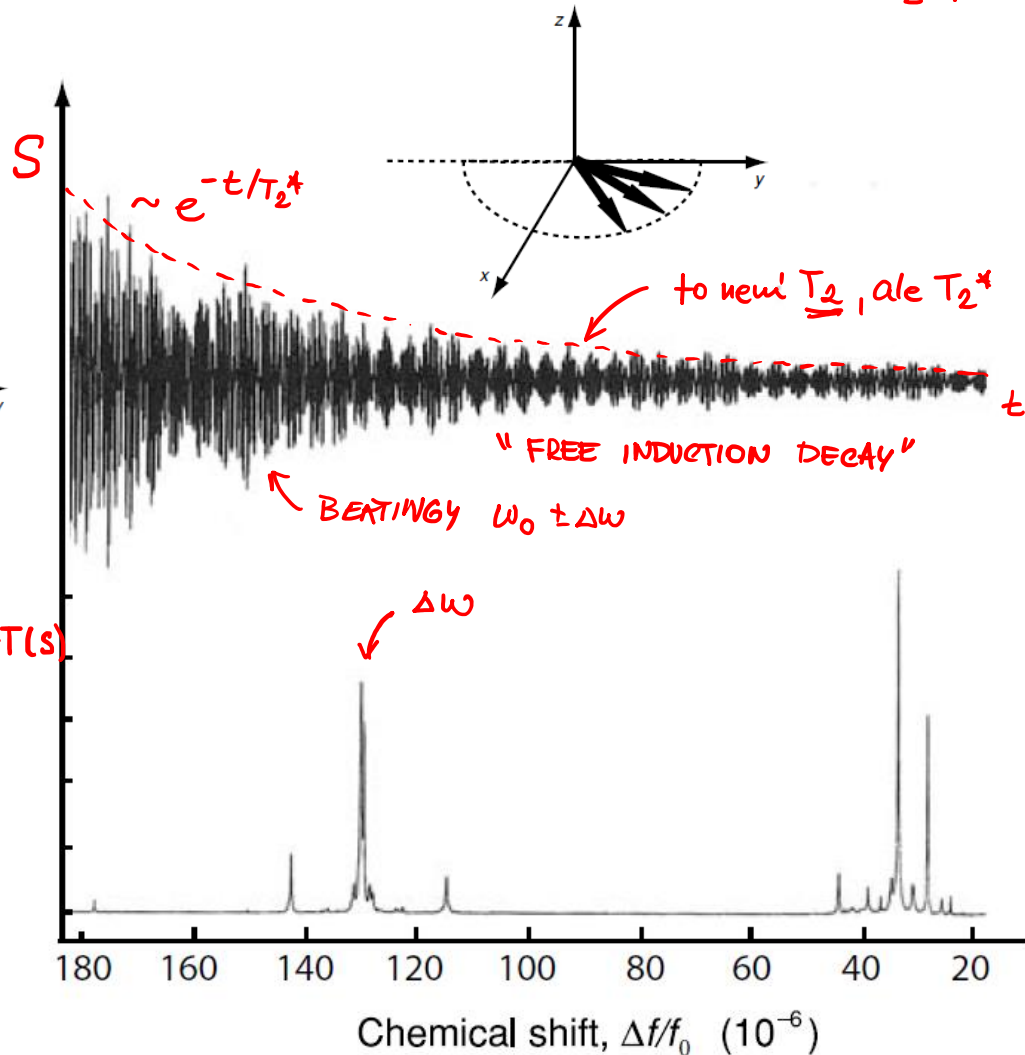
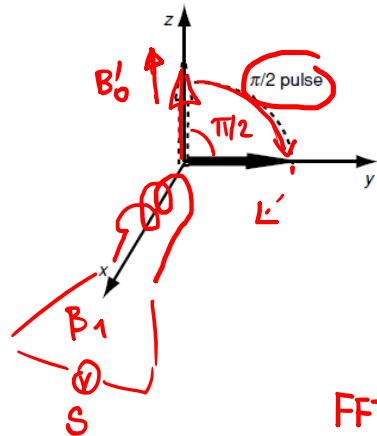
$t_{\pi/2} = \frac{\pi/2}{fB}$

$\pi/2$ -pulz

$t_{\pi} = \frac{\pi}{fB}$

π -pulz

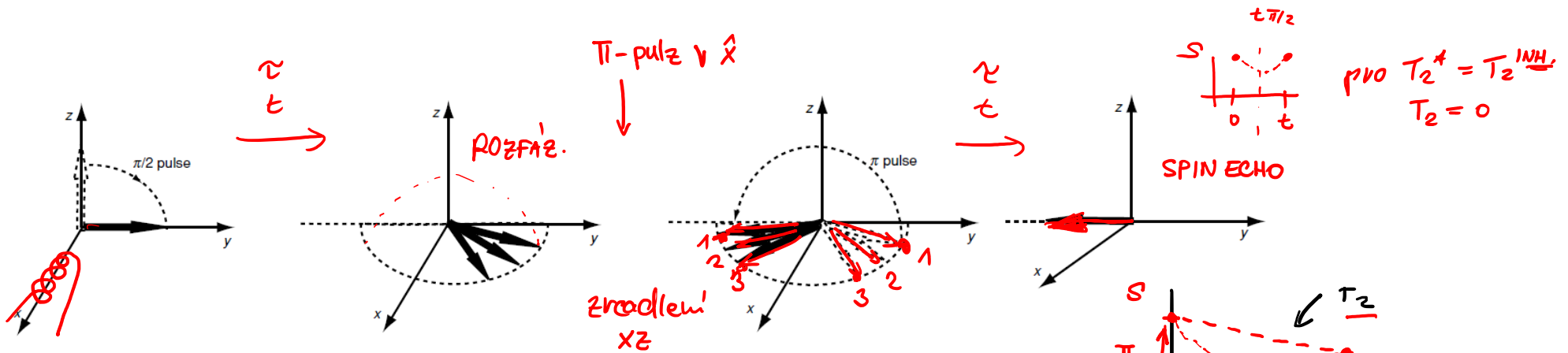
→ pro B_1 :
 RF cívka $\sim \hat{x}$:
 INDUKCE PŮJ PRECESI



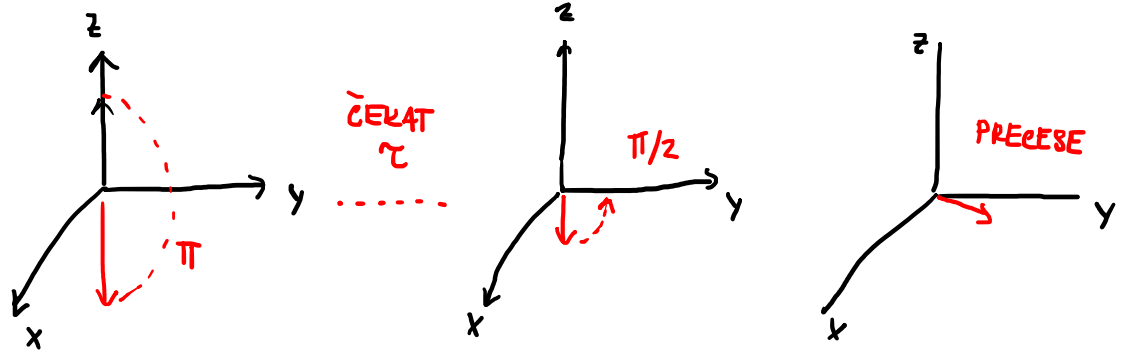
MAGNETICKÁ REZONANCE

PULZNI NMR | ESR...

$T_2 = ?$



$T_1 = ?$



$M_z(t) = S(0)$

MAGNETICKA' REZONANCE

